

YEAR 7 – ALGEBRAIC THINKING... Sequences

What do I need to be able to do?

By the end of this unit you should be able to:

- Describe and continue both linear and non-linear sequences
- Explain term to term rules for linear sequence
- Find missing terms in a linear sequence

Keywords

Sequence: items or numbers put in a pre-decided order

Term: a single number or variable

Position: the place something is located

Rule: instructions that relate two variables

Linear: the difference between terms increases or decreases by the same value each time

Non-linear: the difference between terms increases or decreases in different amounts

Difference: the gap between two terms

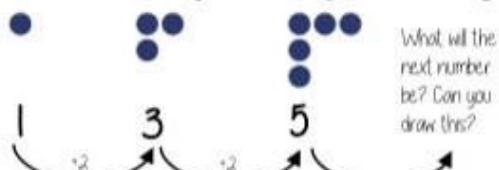
Arithmetic: a sequence where the difference between the terms is constant

Geometric: a sequence where each term is found by multiplying the previous one by a fixed non zero number



Describe and continue a sequence diagrammatically

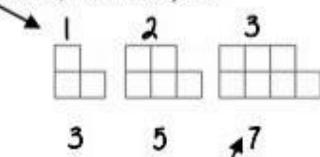
Count the number of circles or lines in each image



What will the next number be? Can you draw this?

Sequence in a table and graphically

Position: the place in the sequence

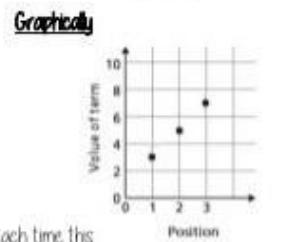


Term: the number or variable (the number of squares in each image)

In a table

Position	1	2	3
Term	3	5	7
	+2	+2	

Because the terms increase by the same addition each time this is **linear** – as seen in the graph



Continue Linear Sequences

7, 11, 15, 19...



How do I know this is a linear sequence?

It increases by adding 4 to each term

How many terms do I need to make this conclusion?

At least 4 terms – two terms only shows one difference not if this difference is constant (a common difference)

How do I continue the sequence?

You continue to repeat the same difference through the next positions in the sequence

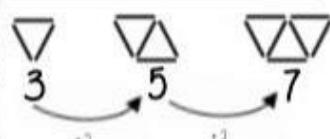
Explain term-to-term rule How you get from term to term

Try to explain this in full sentences not just with mathematical notation

Use key maths language – doubles, halves, multiply by two, add four to the previous term etc

To explain a whole sequence you need to include a term to begin at...

Predict and check terms



CHECK – draw the next terms



Predictions:

Look at your pattern and consider how it will increase.

e.g. How many lines in pattern 6?

Prediction - 13

If it is increasing by 2 each time – in 3 more patterns there will be 6 more lines

Linear and Non Linear Sequences

Linear Sequences – increase by addition or subtraction and the same amount each time

Non-linear Sequences – do not increase by a constant amount – quadratic, geometric and Fibonacci

- Do not plot as straight lines when modelled graphically
- The differences between terms can be found by addition, subtraction, multiplication or division

Fibonacci Sequence – look out for this type of sequence

0 1 1 2 3 5 8 ...

Each term is the sum of the previous two terms



Continue non-linear Sequences

1, 2, 4, 8, 16...



How do I know this is a non-linear sequence?

It increases by multiplying the previous term by 2 – this is a geometric sequence because the constant is multiply by 2

How many terms do I need to make this conclusion?

At least 4 terms – two terms only shows one difference not if this difference is constant (a common difference)

How do I continue the sequence?

You continue to repeat the same difference through the next positions in the sequence

The next term is found by tripling the previous term
The sequence begins at 4

4, 12, 36, 108...

First term